

## MULTIPLE REGRESSION FORMULAS

**For  $k = 2$ :**

$B_{12.3} = (r_{12} - r_{13}r_{23}) / (1 - r_{23}^2)$	standardized partial regression coefficient for variable $z_2$
$B_{13.2} = (r_{13} - r_{12}r_{23}) / (1 - r_{23}^2)$	standardized partial regression coefficient for variable $z_3$
$b_{12.3} = B_{12.3} (s_1/s_2)$	unstandardized partial regression coefficient*
$b_{13.2} = B_{13.2} (s_1/s_3)$	unstandardized partial regression coefficient*
$b_1 = M_1 - b_{12.3} M_2 - b_{13.2} M_3$	intercept (valid for both raw and mean-deviation scores)*
$R^2 = B_{12.3} r_{12} + B_{13.2} r_{13}$	squared multiple correlation*

\*generalizes directly to  $k > 2$  regression equations

**For  $k \geq 2$ :**

$$\text{adj-}R^2 = 1 - (1 - R^2) [(n - 1) / (n - k - 1)]$$

$$\Delta R_j^2 = R_{j \text{ in}}^2 - R_{j \text{ out}}^2 = B_j^2 \text{tol}_j \quad \text{semipartial squared for } j\text{th independent variable}$$

$$\text{where } \text{tol}_j = 1 - R_{j.234\dots(j)\dots m}^2 \quad \text{the proportion of unique variance in } j\text{th variable}$$

$$F_{k, n-k-1} = \frac{R^2 / k}{(1 - R^2) / (n - k - 1)} \quad \text{to test squared multiple correlation}$$

$$F_{1, n-k-1} = \frac{\Delta R_j^2 / 1}{(1 - R^2) / (n - k - 1)} = t^2 \text{ with } df = n - k - 1 \text{ (to test significance of } b_j \text{ or } B_j)$$

$$F_{k', n-k-1} = \frac{\Delta R^2 / k'}{(1 - R^2) / (n - k - 1)}$$

where  $k' = \#$  IVs in subset of variables being added to equation (i.e.,  $k' < k$ )  
and  $\Delta R^2$  is the increment to the  $R^2$  with the addition of that set ( $R^2$  from complete equation).